

# Intrinsic electronic excitations and impurity luminescent centres in NaMgF<sub>3</sub> and MgF<sub>2</sub> doped with Yb<sup>2+</sup>

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## ARTICLE INFO

### Keywords:

Self-trapped exciton  
Impurity-trapped exciton  
Lanthanide  
Ytterbium  
NaMgF<sub>3</sub>  
MgF<sub>2</sub>  
Synchrotron radiation  
VUV spectroscopy

## ABSTRACT

The relaxation pathways of states in the energy region of the fundamental absorption of NaMgF<sub>3</sub>:Yb<sup>2+</sup> and MgF<sub>2</sub>:Yb<sup>2+</sup> are investigated using time-resolved vacuum ultraviolet spectroscopy. For NaMgF<sub>3</sub>:Yb<sup>2+</sup>, excitation into intrinsic free exciton states or above the band gap results in emission features associated with self-trapped excitons and impurity-trapped excitons. Excitation into host-related states of MgF<sub>2</sub>:Yb<sup>2+</sup> similarly exhibits self-trapped exciton emission as well as emission from Yb<sup>2+</sup> 4f<sup>13</sup>5d states. The excitation features related to Yb<sup>2+</sup> 4f<sup>14</sup>→4f<sup>13</sup>5d transitions are interpreted using semi-empirical crystal field models. For both materials, the interplay between intrinsic distortions and Yb impurity centres, as the excitation wavelength and sample temperature are varied, is presented and analysed.

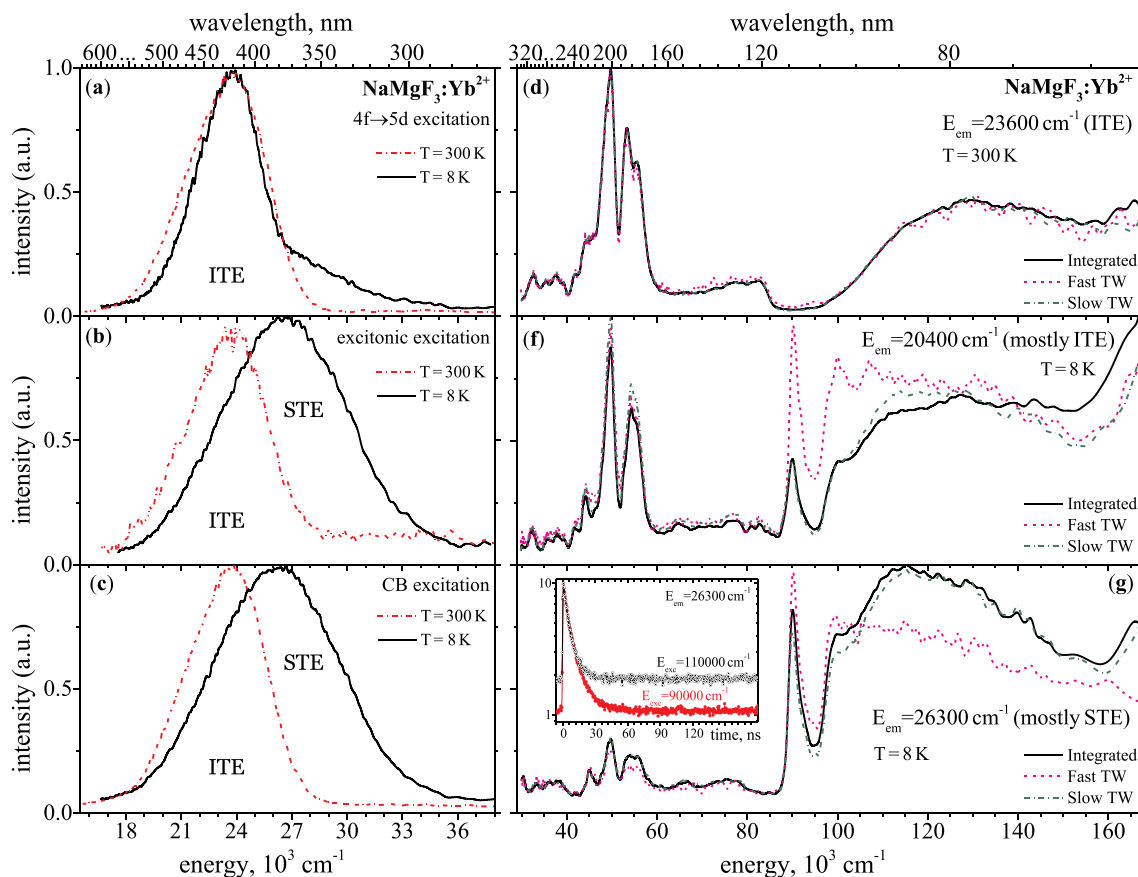
## 1. Introduction

Electronic transitions in lanthanide doped wide bandgap materials include formation and relaxation of *e-h* pairs, excitonic processes, charge exchange or charge transfer transitions, and transitions within a localized impurity ion. Understanding the interplay between the above mentioned fundamental processes may lead to better engineered materials for applications as scintillators or phosphors, in lighting and dosimetry. While the processes related to the relaxation of primary electronic excitations are similar enough in many types of optical wide bandgap materials, the following steps may demonstrate varieties dependent on electronic structure of a particular impurity ion and its interaction with the host. Charge exchange processes occurring between the lanthanide impurity and the host conduction band (CB) may result from photoionization of electron in an excited 5d state through electron-to-donor transitions of the impurity. Ionisation of 5d electron and its delocalization over the next-neighbour metal-ions (so called delocalized Rydberg states) may lead to the formation of impurity-trapped exciton (ITE) where hole moiety remains localized on the impurity. In some cases, the ITE may decay radioactively that results in broad emission band with large Stokes shift. Obviously, formation of ITE is a quenching

process that prevents 4f<sup>13</sup>5d→4f<sup>14</sup> radiative decay. Such process are often referred to 'anomalous emission' and are observed in fluoride crystals doped with Yb<sup>2+</sup>, and in some cases Eu<sup>2+</sup>.

The materials CaF<sub>2</sub>, NaMgF<sub>3</sub> and MgF<sub>2</sub> doped with Yb<sup>2+</sup> have usually been considered as good candidates for studying the ITE related phenomena due to their wide band gaps [1–4]. Previous work on the VUV spectroscopy of CaF<sub>2</sub>:Yb<sup>2+</sup> has shown emission due to both impurity-trapped exciton (ITE) and self-trapped exciton (STE) states with evidence of energy transfer between them [5]. We note that the ITE model itself was recently shown to not fully describe all observations related to anomalous emission in Yb-doped CaF<sub>2</sub> and SrF<sub>2</sub>. A more recent model suggests that this emission is associated with an intervalence charge transfer process associated with the presence of Yb<sup>2+</sup> - Yb<sup>3+</sup> mixed valence pairs [6–10]. These results do not invalidate the ITE model but rather point to complexity of relaxation processes followed 4f<sup>14</sup>→4f<sup>13</sup>5d excitation Yb<sup>2+</sup> ion in fluorites. In this connection it is important to expand our understanding of the spectroscopy and dynamics of Yb<sup>2+</sup> 4f<sup>13</sup>5d excited states in the wider fluoride family. In this work, we focus on time-resolved VUV spectroscopic study of NaMgF<sub>3</sub>:Yb and MgF<sub>2</sub>:Yb single crystals and compare the results to that previously published for CaF<sub>2</sub>:Yb<sup>2+</sup>.

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**Fig. 1.**  $\text{NaMgF}_3:\text{Yb}^{2+}$ . Emission spectra (left panels) recorded in time-integrated mode at  $T = 8\text{ K}$  and  $T = 300\text{ K}$  upon  $4f\text{-}5d$  excitation near  $54000\text{ cm}^{-1}$  (a), excitation into free exciton formation peak at  $90000\text{ cm}^{-1}$  and  $87000\text{ cm}^{-1}$  at  $T = 8\text{ K}$  and  $T = 300\text{ K}$ , respectively (b) and above the band gap at  $117700\text{ cm}^{-1}$ . Excitation spectra (right panels) in time-integrated and time-resolved mode recorded monitoring the ITE emission near  $23500\text{ cm}^{-1}$  (d) and  $20400\text{ cm}^{-1}$  (f) at  $T = 300\text{ K}$  and  $T = 8\text{ K}$ , respectively, and the STE emission near  $26300\text{ cm}^{-1}$   $T = 8\text{ K}$ . Insert in panel (g) shows STE emission decay kinetics recorded upon excitation into free exciton formation peak and above the band gap. See more details on the graphs.

$\text{NaMgF}_3$  is a technologically important material having both mechanical and optical properties which make it a desirable host material for dosimetry applications, in particular. Optically stimulated luminescence (OSL) dosimetry measurements have been performed on  $\text{NaMgF}_3$  doped with divalent europium [11] and trivalent cerium [12]. Finding new materials for applications such as OSL dosimetry is aided by greater understanding of the nature of the phenomena which lead to luminescence in the materials. The broad band emission observed when  $\text{Yb}^{2+}$  ions in  $\text{NaMgF}_3:\text{Yb}$  are excited with UV radiation into its  $4f^{13}5d$  excited configuration is currently accepted to be associated with radiative relaxation from an ITE state [13]. ITEs are formed when a  $5d$  electron becomes delocalized over surrounding cations; effectively -  $\text{Yb}^{3+} + e^-$ . UV excitation studies of  $\text{NaMgF}_3:\text{Yb}^{2+}$  show two overlapping emission peaks associated with ITEs in two different charge-compensation arrangements [13,14].

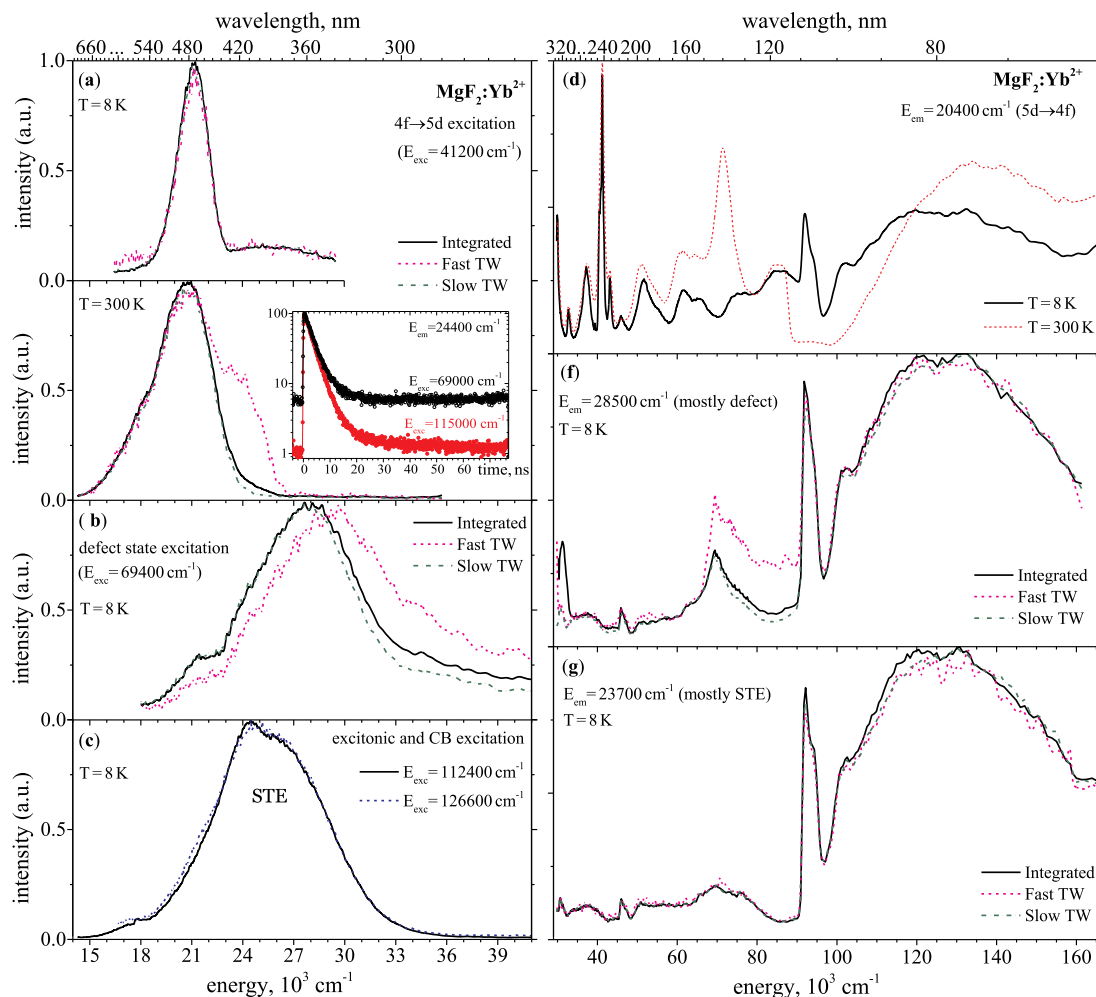
Ultraviolet excitation of  $\text{MgF}_2:\text{Yb}$  also yields a broad visible emission band which has been previously interpreted as ITE emission [15] however recent studies have suggested this to be associated with a regular  $\text{Yb}^{2+} 4f^{13}5d \rightarrow 4f^{14}$  transition.  $\text{MgF}_2:\text{Yb}$  differs from both  $\text{CaF}_2:\text{Yb}$  and  $\text{NaMgF}_3:\text{Yb}$  in that the lowest component of the  $\text{Yb}^{2+} 4f^{13}5d$  excited state sits well below the conduction band. Dorenbos (2003) [16] suggested the emission from  $\text{MgF}_2:\text{Yb}$  deviated from where it would sit in comparison to  $\text{MgF}_2:\text{Eu}^{2+}$  emission by  $\Delta D = -0.26\text{ eV}$  ( $2100\text{ cm}^{-1}$ ), so it was possible that the emission should be classified as “anomalous” and correspond to ITE recombination. In a more recent study, Senanayake [17,18] utilised a UV-IR transient photoluminescence enhancement technique to investigate  $\text{MgF}_2:\text{Yb}$  observing electron trap liberation but no evidence of intra-excitonic transitions. It was concluded that the

emission originated from a  $4f^{13}5d \rightarrow 4f^{14}$  transition. Comparing the emission behaviour of  $\text{MgF}_2:\text{Yb}$  with alkaline earth fluoride hosts which exhibit exciton emission is useful in characterising the difference between emission originating in excitonic and intrinsic transitions and investigating the environmental factors which cause excitons form and decay radiatively.

When alkali earth halides are excited with vacuum ultraviolet radiation into free exciton states, the free excitons self-trap and radiatively recombine producing a broad visible self-trapped exciton (STE) emission band [19]. This work shows the dynamics of relaxation from host electronic states to STE, ITE and  $5d$  Yb states.

## 2. Experimental

The  $\text{NaMgF}_3:\text{Yb}$  and  $\text{MgF}_2:\text{Yb}$  crystals used in this work contained 0.6 mol% of ytterbium and were grown using the Bridgman-Stockbarger technique in a reducing atmosphere. As such, they generally contain a mixture of ions having the divalent and trivalent ionisation states [20]. Absorption spectra were measured using a Cary 6000i spectrophotometer equipped with a temperature controlled, closed cycle cryostat system. The time-resolved VUV spectroscopic measurements were carried out using the SUPERLUMI facility at HASYLAB of DESY (Hamburg, Germany) with synchrotron radiation (SR) from the DORIS III storage ring [21]. The as-grown crystals were cleaved before mounting to the sample holder. A 2 m monochromator in McPherson mounting with a resolution of  $3.2\text{ \AA}$  was used for measurements of excitation spectra in the range of  $30\,000\text{--}170\,000\text{ cm}^{-1}$ . The detection of the luminescence was done with a 0.3 m ARC SpectraPro-308i monochromator equipped



**Fig. 2.** MgF<sub>2</sub>:Yb<sup>2+</sup>. Emission spectra (left panel) recorded in time-integrated and time-resolved mode upon 4f-5d excitation near 41200 cm<sup>-1</sup> (a), within transparency range in presence of 4f-5d and defect absorption at 61300 cm<sup>-1</sup> (b), near defect absorption state at 69400 cm<sup>-1</sup> (c), and into free exciton formation peak at 112400 cm<sup>-1</sup> and above band gap at 126600 cm<sup>-1</sup> (d). Excitation spectra (right panel) were recorded in time-integrated mode for Yb<sup>2+</sup> 5d-4f emission (f), defect emission near 28500 cm<sup>-1</sup> at T = 8 K (f) and STE emission monitored at 23700 cm<sup>-1</sup> at T = 8 K (g).

with a high-speed R3809U-50S (Hamamatsu) microchannel plate (MCP) detector. The time-integrated spectra were recorded by counting the emission signal within the whole time period of 480 ns available between SR pulses at a reduced (2) bunch mode (BM) of the storage ring. The time-resolved spectra were recorded within two time windows (TWs): 4–30 ns (fast time gate) and 248–420 ns (slow time gate) relative to the beginning of the SR pulse. The measurements were performed in the temperature range of 8–300 K in an ultra-high-vacuum chamber (~10<sup>-9</sup> mbar). The excitation spectra were corrected for the wavelength-dependent variation of the SR intensity using a sodium salicylate signal. A background signal corresponding to the dark count of the MCP detector was subtracted from the original spectra and decay curves.

### 3. Results

#### 3.1. Excitation and fluorescence of NaMgF<sub>3</sub>:Yb<sup>2+</sup>

Fig. 1 shows the NaMgF<sub>3</sub>:Yb<sup>2+</sup> emission spectra recorded in time-integrated mode (left panel) and excitation spectra recorded in both time-integrated and time-resolved modes (right panel) at T = 8 K and T = 300 K. Upon excitation into the 4f<sup>13</sup>5d states of Yb<sup>2+</sup> at 41200 cm<sup>-1</sup>,

emission from the ITE is observed as an approximately Gaussian shaped emission band at 23800 cm<sup>-1</sup> with a FWHM of 4210 cm<sup>-1</sup> and 5020 cm<sup>-1</sup> at T = 8 K and T = 300 K, respectively. The ITE is also observed upon excitation into the host (excitonic and CB) states at T = 300 K. For low temperatures, the ITE emission band is obscured by the intense STE emission band (Fig. 1-b, -c). The STE emission is a broad (FWHM ~ 4210 cm<sup>-1</sup>) band centred near 26600 cm<sup>-1</sup> and can only be excited via the formation of free excitons or upon higher energy excitation that corresponds to the generation of separated electron-hole pairs. At T = 300 K, the STE emission is quenched and emission spectra of NaMgF<sub>3</sub>:Yb<sup>2+</sup> recorded upon host excitation, reflect ITE emission only. We note that the emission spectra recorded within fast and slow TWs do not reveal any noticeable deviations from those recorded in time-integrated mode and are not shown for brevity.

The excitation spectra recorded monitoring ITE emission at T = 8 K and T = 300 K demonstrate intense features in the energy range E<sub>exc</sub> < 60000 cm<sup>-1</sup> which are connected to 4f-5d transitions (Fig. 1, d, f). The peak at 90 000 cm<sup>-1</sup> observed in the low-temperature excitation spectrum (Fig. 1f and g) is the free exciton peak which has been reported in reflectance measurements [22]. The presence of the free exciton peak in the excitation spectrum of ITE emission provides direct evidence of energy transfer between intrinsic excitons and Yb<sup>2+</sup>. The most likely

pathway from the formation of free excitons to ITE emission is the formation of STEs and energy transfer from the STEs to the Yb ions. Energy transfer from STEs to luminescent centres has been shown in other materials [23,24] including  $\text{CaF}_2:\text{Yb}^{2+}$  [5].

The absence of the free exciton peak in the 300 K excitation spectrum recorded monitoring the ITE emission may be explained by thermally induced non-radiative relaxation of STE [25] and surface losses [23,26,27]. When the sample is excited above  $95\,000\text{ cm}^{-1}$  the relative intensity of the ITE emission increases. This emission increase suggests that there is also a pathway for host-to-impurity energy transfer involving relaxation of primary  $e-h$  pairs. We note that the relative intensity of the 8K excitation spectrum of the ITE in the range corresponding to direct formation of  $e-h$  pairs is almost double that at the excitonic peak. This is a manifestation of surface quenching where excitons with low kinetic energy are directly created with photons near  $92\,000\text{ cm}^{-1}$  resulting in a low intensity excitonic peak. The efficient energy transfer from  $e-h$  pairs to  $\text{Yb}^{2+}$  will be discussed below, along with results obtained for  $\text{MgF}_2:\text{Yb}^{3+}$ .

In the range of  $128\,000\text{--}156\,000\text{ cm}^{-1}$  the ITE emission excitation spectra recorded at both  $T = 8\text{ K}$  and  $T = 300\text{ K}$  demonstrate a slight decrease of the quantum yield that is likely connected with migration losses due to increased escape during the thermalization stage [26,27]. A similar effect, over a wider energy range, is observed in the excitation spectrum of the STE emission.

The 8 K excitation spectra exhibit significant enhancement of the fast TW signal around the free excitonic peak. The insert in Fig. 1-g shows the emission decay curves recorded monitoring the STE emission band maximum upon excitation into the free exciton peak and above the band gap. The decay curves have a fast component with a time constant of 9 ns and a much slower decay component (tens of microseconds or even longer). The long-time decay component is present as a constant level (piling) due to overlay of the emission decay pulses excited by the continuous sequence of excitation pulses arriving with a high repetition rate (see Ref. [28] for details). The presence of a fast decaying component in the STE emission of  $\text{NaMgF}_3$  was first documented in Ref. [29] and assigned to relaxation of the  $\sigma$  (singlet) component of the STE.

### 3.2. Excitation and fluorescence of $\text{MgF}_2:\text{Yb}^{2+}$

Fig. 2 presents the time-integrated and time-resolved emission spectra as well as the excitation spectra of  $\text{MgF}_2:\text{Yb}^{2+}$  recorded for sample temperatures of  $T = 8\text{ K}$  and  $T = 300\text{ K}$ . When  $\text{MgF}_2:\text{Yb}^{2+}$  is excited into the 5d states at  $E_{\text{exc}} = 41\,200\text{ cm}^{-1}$ , the 8 K emission spectrum is dominated by a relatively broad Pekar-like emission band centred at  $21\,130\text{ cm}^{-1}$  with a FWHM =  $2\,160\text{ cm}^{-1}$ . This emission feature has been previously ascribed to regular  $4f^{13}5d \rightarrow f^{14}$  emission of the  $\text{Yb}^{2+}$  ion [17]. When the temperature is raised to 300K, the emission band slightly red shifts approximately  $500\text{ cm}^{-1}$  and broadens by a factor of two (FWHM  $\sim 3\,940\text{ cm}^{-1}$ ). The emission is dominated by the signal collected in the slow TW at any measured temperature. At temperatures above 200 K, we observe a weak emission band centred around  $23\,400\text{ cm}^{-1}$  that is excited both upon excitation within the transparency range and for direct host excitation. This signal is most pronounced within the fast TW spectrum (Fig. 2-a, lower panel). The insert in Fig. 2-a shows the luminescence decay profiles recorded monitoring the fast emission upon excitation at  $69\,000$  and  $115\,000\text{ cm}^{-1}$  for  $T = 300\text{ K}$ . The fast component in the decay profiles has a decay constant of 3.8 ns. The nature of the fast emission band is not well understood and requires further study that is beyond the scope of this paper. We note, however, that the spectral properties of the fast emission remain those documented for the emission of M-centres in  $\text{MgF}_2$  [30].

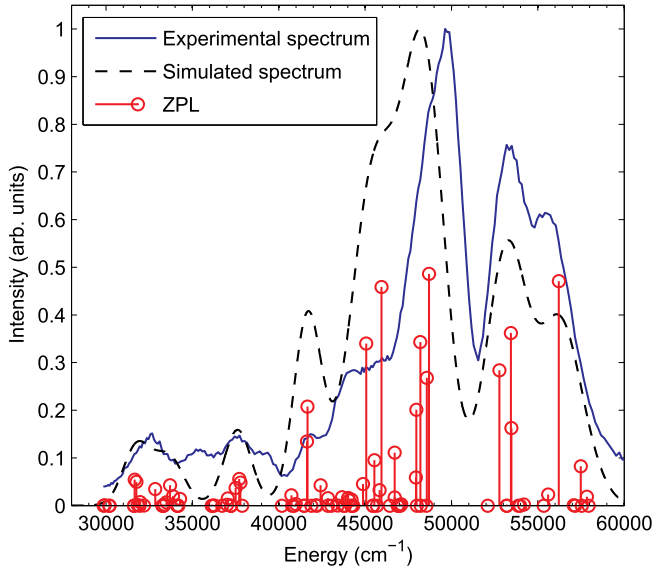
The emission spectrum of  $\text{MgF}_2:\text{Yb}^{2+}$  at  $T = 8\text{ K}$  demonstrates a noticeable dependence on excitation energy (i.e. the ‘optical frequency’ at which excitation occurs). Apart from the above mentioned  $\text{Yb}^{2+} 4f^{13}5d \rightarrow f^{14}$  emission, we observe a broad emission band centred near  $27\,800\text{ cm}^{-1}$  (FWHM  $\sim 7\,870\text{ cm}^{-1}$ ) of quite low intensity excited in the

transparency range (Fig. 2-b) and emission at  $25\,200\text{ cm}^{-1}$  (FWHM  $\sim 7\,320\text{ cm}^{-1}$ ) due to radiative recombination of  $\text{MgF}_2$  STEs from their triplet state (Fig. 2-c) [31]. The band at  $27\,800\text{ cm}^{-1}$  is tentatively assigned to defect emission. The dip near  $22\,100\text{ cm}^{-1}$  at the low energy side of this band results from reabsorption of the emission by  $\text{Yb}^{2+} (4f^{14} \rightarrow 4f^{13}5d)$  - see the experimental and simulated absorption spectra in Fig. 4). We note that upon host excitation at  $T = 8\text{ K}$  the  $\text{MgF}_2:\text{Yb}^{2+}$  emission spectrum is dominated by the STE band that obscures the  $\text{Yb}^{2+}$  and the defect emission features.

The excitation spectra recorded monitoring  $\text{Yb}^{2+} 4f^{13}5d \rightarrow 4f^{14}$  emission at  $T = 8\text{ K}$  and  $T = 300\text{ K}$  are dominated by features related to  $4f^{14} \rightarrow 4f^{13}5d$  absorption transitions in the energy range below about  $67\,000\text{ cm}^{-1}$  (Fig. 2-d). The features observed at higher energy but below the fundamental absorption edge are expected to represent a superposition of high-energy  $4f^{14} \rightarrow 4f^{13}5d$  transitions and defect states. The latter are pronounced in the excitation spectrum for the defect emission at  $27\,800\text{ cm}^{-1}$  as a broad non-uniform excitation feature spread from about  $58\,000$  to  $83\,000\text{ cm}^{-1}$  with a maximum near  $69\,500\text{ cm}^{-1}$  (Fig. 2-f). The peak near  $71\,000\text{ cm}^{-1}$  in the  $\text{Yb}^{2+}$  excitation spectrum at  $T = 300\text{ K}$  and missing at  $T = 8\text{ K}$  (Fig. 2-d) may be connected with thermally assisted defect-to-impurity energy transfer.

The peak at  $92\,000\text{ cm}^{-1}$  observed in  $\text{Yb}^{2+}$  and the defect emission excitation spectra recorded at  $T = 8\text{ K}$  are most pronounced in the excitation spectrum of STE emission (Fig. 2-g) and represents the formation of free excitons [31] as well as indicating the existence of energy transfer from STEs to  $\text{Yb}^{2+}$  and defect states. Similar to the case of  $\text{NaMgF}_3:\text{Yb}^{2+}$ , the STEs in  $\text{MgF}_2$  are thermally quenched at  $T = 300\text{ K}$  thus the excitonic peak is absent in excitation spectrum recorded monitoring the  $\text{Yb}^{2+} 4f^{13}5d \rightarrow 4f^{14}$  emission, for this temperature. Both the  $\text{Yb}^{2+}$  and the defect emission are efficiently excited above the band gap.

The behaviour of the excitation spectra for  $\text{NaMgF}_3:\text{Yb}^{2+}$  and  $\text{MgF}_2:\text{Yb}^{2+}$  in the energy range of the host absorption is quite similar. At low temperature, both materials exhibit efficient energy transfer from optically excited excitons. In fluorides, free excitons typically relax into STEs characterized by a low mobility at low temperature. However, owing to their long lifetimes and the relatively high concentration of impurity ions, that increases the probability of creating excitons in the vicinity of  $\text{Yb}^{2+}$  ions, thus energy transfer via STEs becomes efficient. Reabsorption of STE emission by  $\text{Yb}^{2+}$  is also possible due to the spectral overlap of the STE emission and the lowest energetic  $\text{Yb}^{2+} 4f^{14} \rightarrow 4f^{13}5d$  absorption bands in both crystals. The energy transfer mechanism which occurs for above band gap excitation is likely to be more complicated. The location of the  $\text{Yb}^{2+} 4f^{14}$  ground state in fluorides is expected to be around 9 eV above the top of valence band (VB) [32] that excludes a direct capture of thermalized holes by  $\text{Yb}^{2+}$ . In this case, the exciton mechanism of energy transfer should obviously dominate. This is supported by the similarities in the low temperature excitation spectra when monitoring either STE, ITE or  $\text{Yb}^{2+}$  emission - for excitation above the band gap. At  $T = 300\text{ K}$  the STE emission of  $\text{NaMgF}_3$  and  $\text{MgF}_2$  is quenched as observed in our study and documented in Refs. [28,31]. The thermal quenching of STEs in fluorides is typically ascribed to thermally assisted energy transfer to neighbouring STEs (through exciton-exciton interactions) or decay into point defects like F-H pairs or Frenkel defects [33,34] - this is evident for  $\text{MgF}_2$  [35]. This suggests that a direct energy transfer from STEs to  $\text{Yb}^{2+}$  centres, either via dipole-dipole interactions or reabsorption, should be considered as very inefficient or unlikely at  $T = 300\text{ K}$ . We suppose that under these conditions, the energy transport may be supported by elementary processes such as the relaxation of ultrashort-lived STE precursors (e.g. free excitons or polarons). The efficiency and dynamics of such processes will be dependent upon the spatial distribution of quenchers such as long lived or stationary defects and the energy of exciting photons. To get insight into this, additional experimental and theoretical studies are required. These may include a sub-ns time-resolved study of emission transients similar to that demonstrated in Ref. [36] where the dynamics of STE quenching has been considered and



**Fig. 3.** Excitation spectrum of NaMgF<sub>3</sub>:Yb at 8 K with  $\lambda_{em} = 25000 \text{ cm}^{-1}$  compared to the simulated spectrum calculated with a semi-empirical crystal field model.

theoretical studies based on the modelling of processes controlled by the overlap of wave functions of the interacting states.

### 3.3. Crystal field models of NaMgF<sub>3</sub>:Yb<sup>2+</sup> and MgF<sub>2</sub>:Yb<sup>2+</sup>

The energy levels of the Yb<sup>2+</sup> ion are determined using an effective (or semi-empirical) Hamiltonian, where:

$$H\psi_i = E_i\psi_i \quad (1)$$

$$H_{eff}\varphi_i = E_i\varphi_i. \quad (2)$$

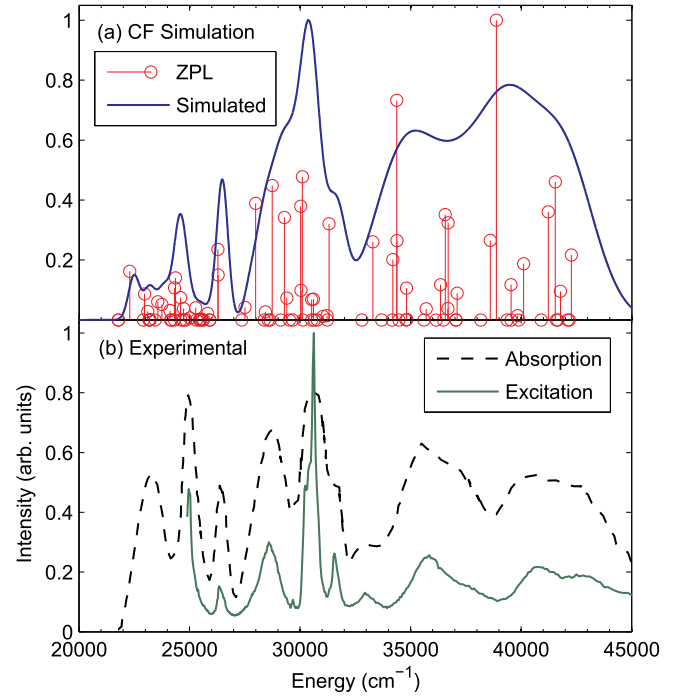
The effective Hamiltonian acts on a reduced ‘model space’ of the full Hamiltonian consisting of only the  $4f^{14} + 4f^{13}5d$  electron configurations of the Yb<sup>2+</sup> impurity. The eigenvalues of the reduced space are the same as for the full Hamiltonian, and hence the energies of these states can be calculated.

The effective Hamiltonian is constructed identically to previous work [37–39], comprising operators representing the Coulomb, spin-orbit and impurity-ligand ‘crystal field’ interactions, weighted by parameters that measure the magnitude of such interactions. Yb<sup>2+</sup> has a ground configuration  $4f^{14}$ , which provides a  $^1S_0$  ground state with energy  $E_{avg}(f)$ . In the excited configuration  $4f^{13}5d$ , there are no two- or three-body interactions between the  $4f$  electrons. The resulting effective Hamiltonian for these  $4f^{14} + 4f^{13}5d$  states is

$$H_{4f^{13}5d} = E_{avg}(f) + \Delta_E(fd) + \zeta(f)A_{so}(f) + \sum_{k=2,4,6} B_q^k(f)C_q^k(f) + \zeta(d)A_{so}(d) \\ + \sum_{k=2,4} F^k(fd)f_k(fd) + \sum_{j=1,3,5} G^k(fd)g_k(fd) + \sum_{k=2,4} B_q^k(d)C_q^k(d). \quad (3)$$

here  $\Delta_E(fd)$  is the average energy of the  $4f^{13}$  configuration relative to  $4f^{14}$ . The  $\zeta(f)$  and  $\zeta(d)$  parameters, and corresponding  $A_{so}$  operators, comprise the spin-orbit effects on the  $4f$  electrons and  $5d$  electron respectively. The  $F^k(fd)$  and  $G^k(fd)$  parameters are the direct and exchange Slater parameters for the Coulomb interaction between electrons in different shells. The  $B_q^k$  parameters describe the crystal field effects for the appropriate electrons.

Which crystal field parameters are included in the parameterised model depends on the geometry of the crystal field. In order to select relevant crystal field parameters, we must assume a structure for the



**Fig. 4.** (a) Simulated spectrum of MgF<sub>2</sub>:Yb calculated with a semi-empirical crystal field model. The red lines are the zero-phonon lines (ZPLs) of the transitions and the blue line is a Gaussian convolution of the ZPLs. (b) Excitation spectrum of MgF<sub>2</sub>:Yb at a sample temperature of 8 K with  $\lambda_{em} = 20400 \text{ cm}^{-1}$  and the room temperature absorption spectrum reported by Küick et al. [40]. (For interpretation of the references to colour in this figure legend, the reader is referred to the Web version of this article.)

Yb<sup>2+</sup> site. The Yb site symmetry was assumed to be a tetragonal distortion from octahedral symmetry for both NaMgF<sub>3</sub>:Yb<sup>2+</sup> and MgF<sub>2</sub>:Yb<sup>2+</sup>. The tetragonal symmetry is represented by crystal field parameters  $B^4$  and  $B^6$  defined such that  $B_4^4 = \sqrt{\frac{15}{4}}B_0^4$  and  $B_4^6 = \sqrt{\frac{7}{2}}B_0^6$ . The tetragonal distortion is represented by the inclusion of a  $B_0^2$  parameter.

Initial values for the free-ion parameters are determined from their definitions, using Hartree-Fock theory to estimate electron radial distribution functions [41]. Initial values for the crystal field parameters are taken from the CaF<sub>2</sub>:Yb<sup>2+</sup> system and reported in our previous work [5]. The direct and exchange Coulomb parameters are held fixed at the values determined by Pan et al. for SrCl<sub>2</sub>:Yb<sup>2+</sup> [38].

Fig. 3 shows the  $4f^{14} \rightarrow 4f^{13}5d$  excitation spectrum of NaMgF<sub>3</sub>:Yb<sup>2+</sup> (measured at a sample temperature of 8 K) along with a simulated spectrum calculated with the semi-empirical crystal field model. The crystal field parameters were qualitatively fitted to the vacuum ultraviolet experimental spectrum.

As for NaMgF<sub>3</sub>:Yb<sup>2+</sup>, the  $4f^{14} \rightarrow 4f^{13}5d$  transitions of MgF<sub>2</sub>:Yb<sup>2+</sup> can be approximated with a semi-empirical model of the crystal field where the site symmetry is assumed to be octahedral having a tetragonal distortion. The UV-VUV absorption spectrum (up to about  $67000 \text{ cm}^{-1}$ ) of MgF<sub>2</sub>:Yb<sup>2+</sup> has been previously measured by Küick et al. [40]. The absorption spectrum has substantially different relative intensities between peaks when compared to the excitation spectrum (or fluorescence detected absorption spectrum), indicating that absorption into some Yb<sup>2+</sup>  $5d$  levels does not result in efficient ITE emission. Fig. 4 shows the  $4f^{14} \rightarrow 4f^{13}5d$  experimental spectra for MgF<sub>2</sub>:Yb<sup>2+</sup> along with a simulated spectrum calculated with the semi-empirical crystal field model. Since the calculation models the absorption process, the crystal field parameters were qualitatively fitted to the absorption spectrum rather than the excitation spectrum. The values of the crystal field parameters are given in Table 1.

Table 1 contains the values of the crystal field parameters calculated

**Table 1**

Final values of parameters for the crystal field fit of  $\text{Yb}^{3+}$  in  $\text{NaMgF}_3$  and  $\text{MgF}_2$ . All parameter values are given in  $\text{cm}^{-1}$ .

Parameter	Free $\text{Yb}^{2+}$ Ion <sup>a</sup>	$\text{SrCl}_2$ : $\text{Yb}^{2+b}$	$\text{CaF}_2$ : $\text{Yb}^{2+c}$	$\text{NaMgF}_3$ : $\text{Yb}^{2+}$	$\text{MgF}_2$ : $\text{Yb}^{2+}$
$\Delta_E(fd)$		38832	42700	42800	42000
$\zeta(ff)$	1290	1211	1204	2000	3000
$\zeta(dd)$	2899	2950	2950	2700	1000
$F^2(fd)$	23210	14355	14355	14355 <sup>d</sup>	14355 <sup>d</sup>
$F^4(fd)$	10646	7222	7222	7222 <sup>d</sup>	7222 <sup>d</sup>
$G^1(fd)$	10059	4693	4693	4693 <sup>d</sup>	4693 <sup>d</sup>
$G^3(fd)$	8046	5382	5382	5382 <sup>d</sup>	5382 <sup>d</sup>
$G^5(fd)$	6085	4349	4349	4349 <sup>d</sup>	4349 <sup>d</sup>
$B_0^2(ff)$				-700	-1000
$B^4(ff)^e$		-725	-2036	500	1000
$B^6(ff)^f$		292	821	-200	-200
$B_0^2(dd)^e$				-6000	8000
$B^4(dd)^e$		-20442	-37726	22000	40000

<sup>a</sup> Ref [41].

<sup>b</sup> Ref [37].

<sup>c</sup> Ref [5].

<sup>d</sup> Not fitted here. Held at the values determined by Ref. [37].

$$^e B_0^4 = B^4, B_{\pm 4}^4 = \sqrt{\frac{5}{14}} B^4.$$

$$^f B_0^6 = B^6, B_{\pm 4}^6 = -\sqrt{\frac{7}{2}} B^6.$$

from their definitions for the free  $\text{Yb}^{2+}$  ion; those fitted to  $\text{SrCl}_2$ : $\text{Yb}^{2+}$  and  $\text{CaF}_2$ : $\text{Yb}^{2+}$  using a  $4f^{14} \rightarrow 4f^{13}5d$  effective Hamiltonian; and the values of parameters fitted here. The Coulomb parameters have little effect on the spectrum, and are kept at the same value for all three crystal environments. The value of the  $B^4$  and  $B^6$  parameters for  $\text{NaMgF}_3$ : $\text{Yb}^{2+}$  are smaller than for  $\text{CaF}_2$ : $\text{Yb}^{2+}$ .

#### 4. Conclusion

A temperature dependent time-resolved spectroscopic study of bulk single crystals of  $\text{NaMgF}_3$ : $\text{Yb}^{2+}$  and  $\text{MgF}_2$ : $\text{Yb}^{2+}$  has been performed using UV-VUV synchrotron radiation. Emission from ITE or  $\text{Yb}^{2+} 4f^{13}5d$  states has been identified in the both materials. Excitation of the fundamental inter-band absorption of the respective crystals results in emission from intrinsic states and  $\text{Yb}^{2+}$  impurity centres. The interplay between intrinsic states and  $\text{Yb}^{2+}$  impurity centres is observed and analysed as a function of excitation wavelength and sample temperature.

$\text{NaMgF}_3$ : $\text{Yb}^{2+}$  was found to demonstrate similar relaxation pathways upon UV-VUV excitation to that previously published for  $\text{CaF}_2$ : $\text{Yb}^{2+}$  [5]. However, unlike  $\text{CaF}_2$ : $\text{Yb}^{2+}$  where the ITE and STE emission bands are separated by about  $17000 \text{ cm}^{-1}$ , in  $\text{NaMgF}_3$ : $\text{Yb}^{2+}$  the emission bands from ITE and STE states noticeably overlap each other. Emission and excitation features observed for  $\text{MgF}_2$ : $\text{Yb}^{2+}$  in the host transparency range are similar to those previously documented in Refs. [13,17,27] apart from the observation of a weak emission feature near  $23400 \text{ cm}^{-1}$  that has been tentatively assigned to a defect emission.

The lower-energy section of the excitation spectra of  $\text{NaMgF}_3$ : $\text{Yb}^{2+}$  and  $\text{MgF}_2$ : $\text{Yb}^{2+}$  are dominated by the  $\text{Yb}^{2+} 4f^{14} \rightarrow 4f^{13}5d$  transitions. These spectra were qualitatively fitted to a semi-empirical crystal field model where the  $\text{Yb}^{2+}$  site geometry was assumed to have a tetragonal symmetry. The crystal field parameters were compared to previous work on  $\text{CaF}_2$  and  $\text{SrCl}_2$ . The  $B^4$  parameters for  $\text{NaMgF}_3$ : $\text{Yb}^{2+}$  and  $\text{MgF}_2$ : $\text{Yb}^{2+}$  have the opposite sign to  $\text{CaF}_2$ : $\text{Yb}^{2+}$  and the magnitudes of the crystal field parameters are significantly lower for  $\text{NaMgF}_3$ : $\text{Yb}^{2+}$ .

Both materials exhibit quite similar properties in terms of the host-to- $\text{Yb}^{2+}$  energy transfer. In particular, an efficient excitonic energy transfer is observed at  $T = 8 \text{ K}$  either upon excitation into the free exciton

absorption band or above the band gap that is followed by the relaxation of separated e-h pairs into excitons and further to STEs. The latter may also transfer their energy via reabsorption of emission. At  $T = 300 \text{ K}$  the energy transfer is likely to be driven by STE precursors; ultrashort-living electronic excitations existing within a sub-nanosecond time scale after the host excitation.

#### Author declaration

The authors of this manuscript have all read and agreed to the submission of this manuscript.

#### Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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